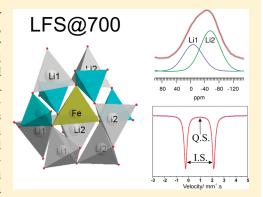
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Li₂FeSiO₄ Polymorphs Probed by ⁶Li MAS NMR and ⁵⁷Fe Mössbauer Spectroscopy

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Supporting Information

ABSTRACT: Several samples of pure Li₂FeSiO₄ polymorphs, prepared by hydrothermal synthesis and then quenched from either 400 °C (*Pmn*2₁), 700 °C (*P2*1/*n*), or 900 °C (*Pmnb*), were thoroughly investigated by Mössbauer and NMR spectroscopy. ⁵⁷Fe Mössbauer spectroscopy showed that (i) iron in all the polymorphs existed in the divalent oxidation state, and (ii) chemical shifts and quadrupolar splittings correlated well with Fe—O bond lengths. ⁶Li MAS NMR spectra of the three different polymorphs exhibit substantially different spinning-sideband patterns and slightly different isotropic shifts. The sideband patterns stemming from the anisotropic electron—nucleus dipole—dipole interaction reflect the arrangement of paramagnetic iron ions around lithium nuclei and allowed unambiguous assignments of ⁶Li MAS NMR signals to crystallographically nonequivalent Li sites. Analysis of isotropic NMR shifts of ⁶Li nuclei revealed that they comprised two contributions of comparable magnitude, a



hyperfine (contact) shift and a pseudo-contact shift. Based on the structural models of Li₂FeSiO₄, both contributions could be successfully predicted by first-principles calculations. The contact shift was obtained from the hyperfine-coupling constant on ⁶Li nuclei, which was calculated within a DFT/PAW approach, and the pseudo-contact shift was derived from the electron—nucleus dipolar matrix and the *g*-tensor, which was computed within the DFT/GIPAW frame.

KEYWORDS: Mössbauer spectroscopy, MAS NMR, DFT/GIPAW, Li₂FeSiO₄, Li-ion batteries

■ INTRODUCTION

The interest in polyanionic materials as positive electrode materials for Li-ion batteries has increased dramatically after the first report on the electrochemical activity of LiFePO₄. Oxygen atoms in the polyanionic framework structures are stabilized by X–O bonds (X = P, Si, B, ...) with a strong covalent nature. This makes polyanionic-based materials safer and more stable over prolonged cycling. An attractive member of this group is $\text{Li}_2\text{FeSiO}_4$ (LFS), 2,3 which is built on inexpensive and abundant raw materials. In recent works, small particles of LFS and proper electrode engineering have yielded electrodes with good cycling stability close to theoretical capacity. 4,5

Besides addressing the challenge of enhancing the electrochemical performances of $\rm Li_2FeSiO_4$ cathodes, the objective of our research is to attempt to understand the complex polymorphism of these silicates and correlate the structural informations obtained with the observed response upon $\rm Li^+$ extraction/insertion. Global (crystal structures, extended, or localized defects) as well as local (Fe and Li environments, connectivity and orientations of $\rm AO_4$ tetrahedra) structural parameters may indeed play a

role for the thermodynamics and kinetics of Li^+ extraction from these structures.

Several polymorphs were recently isolated and characterized, based on careful X-ray diffraction (XRD) and neutron diffraction studies and transmission electron microscopy (TEM) investigation. The proposed structural models for LFS were derived from Li₃PO₄ structures and can be roughly divided into two large subgroups: a low-temperature group (denoted as β), and a high-temperature group (denoted as γ). In both structural models, half of the tetrahedral sites, generated by a distorted hexagonal close packing of oxygen atoms, are occupied by cations, and the difference between polymorphs lies in the respective orientations of the filled tetrahedra and in their connectivity.

The above-described differences among the LFS polymorphs are generally observed in well-crystalline samples, while in

Received: November 7, 2010 Revised: March 19, 2011 Published: May 13, 2011

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the samples prepared for the electrochemical characterization (with particles below 50 nm) or in the samples where a mixture of polymorphs is present, lower-quality XRD patterns may not enable a reliable determination of the structure. In such cases, the use of characterization techniques that can detect local environments of cations in the samples (for instance, NMR or Mössbauer spectroscopy) is of primary importance.

Meaningful parameters such as chemical shift (IS) and quadrupole splitting (QS) can be derived from Mössbauer spectra and provide information about iron coordination, valence state, and covalency of the iron—ligand bonds. It is generally accepted that, for a given oxidation state and for identical ligands, an increase in the covalency of the iron—ligands bonds corresponds to a decrease in the iron—ligands interatomic distances, which is translated to an observed decrease in the isomer shift.¹¹

Nuclear magnetic resonance (NMR) spectroscopy has been used as a characterization technique for many lithium-containing materials for Li batteries. Lithium NMR spectroscopy was particularly useful for the elucidation of structural motifs that did not exhibit long-range order and, thus, could not be analyzed by diffraction techniques. Recently, MAS NMR spectroscopy of Li nuclei has proved to be a very convenient tool that could distinguish between different Li₂MnSiO₄ polymorphs. Lithium nuclei within polymorphs of Li₂MnSiO₄ or lithium nuclei occupying nonequivalent crystallographic lithium sites within a single polymorph exhibited NMR signals at different and well-resolved isotropic positions.

Several structural issues related to tetrahedral lithium-containing transition-metal silicates or phosphates have been studied by first-principles calculations. $^{17-20}$ For example, density-functional theory (DFT)-based calculations were able to predict the stability of pure Li₂MnSiO₄ polymorphs ¹⁷ and of Li₂Fe₂Mn₁₋₂SiO₄ solid solutions.²⁰ In many cases, first-principles calculations also helped in the interpretation of NMR data—in particular, those related to the isotropic shifts detected in ⁶Li or ⁷Li NMR spectra. 21-23 Since isotropic shifts are governed by the magnitude of hyperfine coupling between the magnetic moments of the unpaired electronic spins and the nuclear magnetic moments of Li or Li nuclei, the accuracy of predictions depends predominantly on the accuracy of the determination of electronic spin density at the position of the above-mentioned nuclei. It was shown that very good predictions of hyperfine coupling constants and isotropic shifts could be obtained using DFT, pseudo-potentials, and the Projector Augmented-Wave (PAW) approach. 16,24

In this work, we have used ⁵⁷Fe Mössbauer spectroscopy and ⁶Li solid-state MAS NMR spectroscopy to investigate Li₂FeSiO₄ polymorphs. A systematic study on several samples prepared at different temperatures has been performed. The analysis of NMR spectra has been complemented by first-principles calculations of hyperfine coupling constants and elements of the *g*-tensor. The obtained results are correlated with the structural models determined in our recent publications. ^{7,8} The knowledge about the local structure of the Li₂FeSiO₄ polymorphs, and about the spectroscopic methods to investigate this structure, has been used for the characterization of a typical carbon-coated Li₂FeSiO₄ sample prepared at 700 °C and slowly cooled to room temperature.

■ EXPERIMENTAL SECTION

Different LFS polymorphs were prepared by annealing pristine hydrothermally prepared LFS samples in sealed stainless steel tubes filled with an argon atmosphere. Samples were heated for 6 h at selected temperatures (400, 700, and 900 °C) and quenched to 25 °C. The detailed synthesis procedure is described in ref 8. A typical sample for electrochemical characterization was prepared by mixing citric acid (1.3 g) and an as-prepared hydrothermal sample (1 g). It was heattreated at 700 °C in a CO/CO₂ atmosphere for 6 h and slowly cooled to room temperature.

Powder X-ray diffraction (XRD) patterns of as-prepared LFS polymorphs were measured using Cu $K\alpha_{1,2}$ radiation at 298 K. The machine was equipped with a LinxEye detector that allows energy discrimination (to remove part of the fluorescence). The data were recorded in the 2θ range of $10^\circ-90^\circ$ with a 2θ step size of $\sim\!0.02^\circ$ and with a constant counting time of 12 s per step. The patterns were analyzed by full pattern matching and Rietveld refinements, as implemented in the Fullprof program. 25

⁵⁷Fe Mossbauer experiments were performed in transmission geometry at 298 K. The source was ⁵⁷Co in a Rh matrix. Velocity calibration and isomer shifts (IS) were quoted relative to an absorber of metallic iron at room temperature. Parameter fits were performed using a standard least-squares fitting routine with Lorentzian lines.

Differential thermal analysis was performed over a range of $25-950\,^{\circ}\mathrm{C}$ under a constant flow of argon, using a Simultaneous Thermal Analyzer STA 449 $^{\circ}\mathrm{C}$ Jupiter (from Netzsch), and a heating/cooling rate of $10\,^{\circ}\mathrm{C}$ min $^{-1}$.

Solid-state ⁶Li magic-angle spinning (MAS) NMR spectra were recorded on a 600 MHz Varian NMR system, operating at a ⁶Li Larmor frequency of 88.274 MHz, with a rotation-synchronized Hahn-echo pulse sequence. The sample rotation frequency was 20 kHz, the repetition delay between consecutive scans was 0.1 s, and the number of scans was 15 000. Frequency axis (in ppm) is reported relative to the lithium signal of a 1 M LiCl solution. Spinning-sideband powder patterns were analyzed using the Spinevolution simulation package²⁶ and "dmfit" software.²⁷ In addition to electron—nucleus dipolar interaction, electric quadrupolar interaction was also considered when fitting the spectra of ⁶Li nuclei.

First-principles calculations were performed using the density functional theory (DFT) in the generalized gradient approximation of Perdew—Burke—Ernzerhof (GGA PBE) 28 with plane-wave basis and norm-conserving pseudo-potentials. In the first step, the atomic coordinates of atoms within LFS polymorphs were relaxed and optimized with Quantum Espresso's *pwscf* program. 29 The "final" ground state energies were then recalculated with the optimized geometries. In all calculations, the plane-wave cutoff energy was 1360 eV. The reciprocal-space sampling was performed with k-point grids of 4 \times 4 \times 4 points. All-electron information was reconstructed using the Projector Augmented-Wave (PAW) 16,24 and Gauge-Including Projector Augmented-Wave (GIPAW) 30,31 methods, as implemented in Quantum Espresso's GIPAW module. 29 The module yielded hyperfine coupling constants and elements of g-tensors, which were then used for quantitative prediction of the isotropic shifts.

■ RESULTS AND DISCUSSION

In our recent works, 7,8 we showed that at least three polymorphs of Li₂FeSiO₄ can be isolated through careful quenching procedures. A stoichiometric sample without impurities prepared by hydrothermal synthesis can serve as a good starting point for the isolation of different LFS polymorphs at different temperatures. Thermogravimetric data (Figure 1a) showed a small loss of mass in the temperature range up to 300 °C, related to the desorption of physically and chemically adsorbed water. The

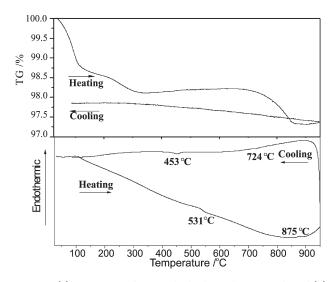


Figure 1. (a) TGA curve of pristine hydrothermal LFS sample and (b) corresponding normalized DSC data during heating and cooling processes at 10 °C/min under an argon atmosphere.

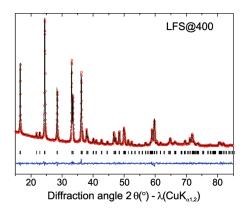


Figure 2. Rietveld refinement of the powder X-ray diffraction (XRD) pattern of LFS@400 ($Pmn2_1$ space group, a = 6.267(4) Å, b = 5.335(2) Å, c = 4.965(3) Å).

reason for the additional loss of mass in the temperature range of 700-800 °C is not clear at the present stage. More important information is obtained from the DSC data (Figure 1b), where exothermic peaks during heating and endothermic peaks during cooling clearly delimit the stability ranges of the three polymorphs. The DSC diagram upon heating displays a steep curve, because of the agglomeration of small initial particles, which hinders the possibility of precise determination of the phasetransition enthalpies. The low-temperature polymorph β (Pmn2₁) transforms to the high-temperature polymorph γ_s (P2₁/n) at a temperature of \sim 530 °C. The phase-transition temperature from the γ_s polymorph to the γ_{II} (*Pmnb*) polymorph was determined to be close to 875 °C upon heating. The phase transitions are reversible throughout the cooling process with the temperature of \sim 724 °C for transition from the $\gamma_{\rm II}$ polymorph to the $\gamma_{\rm s}$ polymorph, and ~453 °C for the transition from the $\gamma_{\rm s}$ polymorph to the β polymorph. Using the DSC data, we have isolated three different samples by quenching as-prepared hydrothermal samples sealed in stainless steel tubes filled with argon from 400 °C (LFS@400), 700 °C (LFS@700), and 900 °C (LFS@900) to 25 °C.

Table 1. Atomic Coordinates, Occupancies and Reliability Factors Obtained by Rietveld Refinement of XRD Data for LFS@400 (Space Group *Pmn*2₁)^a

LFS@400										
site	Wyckoff	occupancy	\boldsymbol{x}	у	z					
Li1	4b	1	0.754(2)	0.334(3)	0.988(1)					
Fe1	2a	1	0	0.1740(1)	0.450(2)					
Si	2a	1	0	0.8260(3)	0.966(1)					
O1	2a	1	0	0.8209(3)	0.314(4)					
O2	2a	1	0	0.1147(4)	0.893(3)					
O3	4b	1	0.789(0)	0.6795(1)	0.871(3)					
a = .		(- (- (()		1 1 7 22 72 (7) 1						

^a Lattice parameters: a = 6.2674(6) Å, b = 5.3352(7) Å, c = 4.9653(5) Å. $R_f = 6.29\%$, V/z = 83.013. Twin mirror at Z = 0.956(1) with 0.68 multiplicity of predominant image.

Table 2. Selected Bond Lengths and Angles of the LFS@400 Sample

	O1	O2	O3	O3				
LiO ₄								
O1	1.992(2)	105.7(4)	107.3(2)	110.8(3)				
O2	3.176(3)	1.991(2)	108.6(2)	113.6(4)				
O3	3.156(1)	3.181(2)	1.925(0)	110.3(2)				
O3	3.238(3)	3.292(1)	3.173(3)	1.941(2)				
${ m SiO_4}$								
O1	1.731(1)	104.09(3)	106.53(3)	106.53(3)				
O2	2.614(1)	1.582(1)	114.02(5)	114.02(5)				
O3	2.676(0)	2.674(3)	1.606(3)	110.80(4)				
O3	2.676(0)	2.674(3)	2.644(5)	1.606(3)				
$\mathrm{FeO_4}$								
O1	2.000(2)	101.47(4)	107.49(5)	107.49(5)				
O2	3.273(2)	2.223(2)	104.3(2)	104.3(2)				
O3	3.234(4)	3.346(4)	2.011(0)	128.49(3)				
О3	3.234(4)	3.346(4)	3.622(3)	2.011(0)				

All samples were checked via Rietveld refinement of powder XRD patterns. The refinements of LFS@700 and LFS@900 were based on the structural models that were recently reported in the literature $^{6-8}$ and are given in the Supporting Information. The structural model for LFS@400 was obtained using the coordinates of β -Li₃PO₄ and Li₂MnSiO₄. The calculated versus experimental plots are given in Figure 2; the atomic coordinates, lattice parameters, and reliability factors are given in Table 1, and the bond lengths and angles are given in Table 2.

A close look at the local environments of Fe^{2+} in each polymorph reveals interesting differences. In all polymorphs, Fe^{2+} atoms are in tetrahedral coordination, surrounded by two LiO_4 tetrahedra, by one FeO_4 tetrahedron, and by one SiO_4 tetrahedron. The differences between iron environments are in the connectivity and in the orientations of the tetrahedra. In LFS@400 sample ($Pmn2_1$ space group), all tetrahedra share corners, and they are all pointing in the same direction along the *c*-axis (Figure 3a). The structures of the high-temperature polymorphs (LFS@700 and LFS@900) are more complicated. In the $P2_1/n$ (LFS@700) phase FeO_4 shares one edge with LiO_4 tetrahedron (Figure 3b), whereas in the Pmnb one (LFS@900) FeO_4 shares

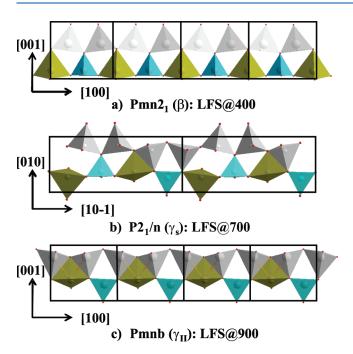


Figure 3. Comparisons between the tetrahedral orientations along equivalent directions in (a) LFS@400, (b) LFS@700, and (c) LFS@900.

two edges with LiO₄ tetrahedra (Figure 3c). The orientation of tetrahedra in the high-temperature polymorphs alternates in their pointing direction: up-up-down-down-up-up-down-down for the $P2_1/n$ structure (LFS@700) and up-down-up-downup-down-up-down for the *Pmnb* structure (LFS@900). The alternation of Fe and Si (Fe-Si-Fe-Si-Fe) is common for all three structures. Differences in the tetrahedra connectivity and in the orientation have an influence on the average bond length in the FeO₄ tetrahedra. The general trend observed is a decrease of the average Fe-O bond length from 2.061(3) Å in LFS@400 to 2.026(1) Å in LFS@900 with intermediate value (2.032(1) Å) for LFS@700. Based on the crystallographic data, an opposite correlation was determined for the distortion of FeO₄ tetrahedra. The largest distortion was found in the LFS@900 sample $(12.8 \times 10^{-4} \, \text{Å}^3)$ and the smallest in LFS@400 sample $(2.3 \times 10^{-4} \text{ Å}^3)$, while the distortion in the LFS@700 sample was $9.9 \times 10^{-4} \text{ Å}^{3.35}$

Mössbauer Spectroscopy

Those significant variations in the local environments of FeO₄ tetrahedra among all Li₂FeSiO₄ polymorphs can be addressed through Mössbauer spectroscopy, as previously reported for iron oxides and iron fluorides. 11 The Mössbauer spectra of the three polymorphs used in this work are gathered in Figure 4 and give a precious information on the quality of the samples investigated: only LFS@400 showed traceable amount of additional iron (below 2 at. %) in different local environments. In addition, the samples do not contain any detectable traces of Fe^{III}- or other Fe^{II}-containing oxides, contrary to what had been reported by Thomas et al.² The parameters (isomer shift and quadrupole splitting) of fitted spectra are within the ranges commonly observed for Fe in tetrahedral coordination 11 but are significantly different from one sample to another. Noticeably, each spectrum could be fitted nicely (χ^2) within a range of 3σ) with only one contribution from Fe, in full accordance with the crystal

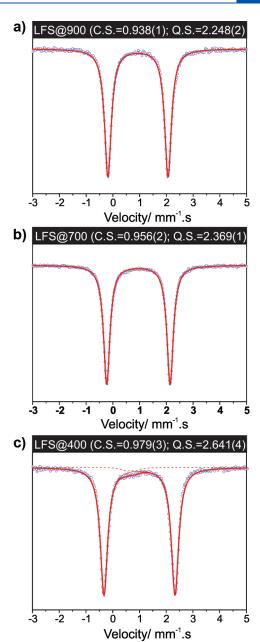


Figure 4. Mössbauer spectra for (a) LFS@900, (b) LFS@700, and (c) LFS@400 samples.

structures of the three polymorphs, each of them comprising only one Fe crystallographic site.

Interestingly, the respective chemical shifts of the three samples follow a general trend observed in other systems: 11 the increase in the covalent nature of the Fe-O bond (decrease in the average bond length) translates to a smaller chemical shift, from 0.94 mm s $^{-1}$ (LFS@900) to 0.98 mm s $^{-1}$ (LFS@400) (Figure 4). Those observations were validated for many samples and are reproducible (see Figure 5).

Even larger differences between samples were observed when comparing the quadrupole splitting values, which can be strongly correlated to the degree of the distortion of the FeO₄ tetrahedra, as reported by Dyar et al. for Fe in staurolite samples.³⁶ The trend of smaller quadrupole splitting for a higher distortion, observed here, cannot be taken as a general one in Mössbauer

spectroscopy but can be used in a particular system where Fe²⁺ have the same type and number of ligands.

■ ⁶Li MAS NMR

As in our recent work on Li₂MnSiO₄, ¹⁶ we measured the ⁶Li MAS NMR spectra on different Li₂FeSiO₄ polymorphs in order to strengthen the information about the local structure, gathered so far through diffraction (electron, X-ray, neutron) and Mössbauer spectroscopy. The NMR spectra of LFS@400, LFS@900, and LFS@700 are shown in Figure 6. All three spectra exhibit broad spinning-sideband patterns that reflect the strong anisotropic dipolar interactions of lithium nuclei with electronic spins of paramagnetic centers, which are predominantly Fe ions

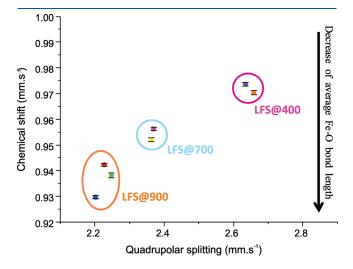


Figure 5. Relationships between quadrupole splitting (QS) and chemical shift (IS) for LFS polymorphs prepared at different temperatures (only samples without detectable impurities were used in this study).

(and, to a smaller extent, if electronic spins are partly delocalized, also O ions). Compared to lithium NMR signals of Li₂MnSiO₄ polymorphs, individual centerbands and sidebands in spectra of LFS polymorphs are $\sim\!10$ times broader. While the full width at half maximum (fwhm) of the former was $\sim\!6-7$ ppm, the fwhm of the latter is $\sim\!60-70$ ppm. The difference in linewidths cannot be attributed to different relaxation rates, because ^6Li T₂ relaxation times of all Li₂MnSiO₄ and Li₂FeSiO₄ polymorphs are almost the same; they are $\sim\!3$ ms long and correspond to linewidths of $\sim\!1$ ppm. Therefore, the much-stronger broadening of the centerbands and sidebands in the spectra of Li₂FeSiO₄ must be produced via another mechanism, most probably by the anisotropic bulk magnetic susceptibility effect, as discussed later in the text.

LFS@400 and LFS@900 samples both exhibit a single lithium contribution with isotropic positions of -72 and -30 ppm, respectively. This is consistent with the proposed crystal structures for Pmn2₁ (LFS@400) and Pmnb (LFS@900) polymorphs, which both contain a single lithium site within their asymmetric crystallographic units. On the other hand, the spectrum of LFS@700 can be decomposed into two equally strong contributions (intensity ratio of 0.49:0.51). The isotropic positions of the two contributions are -7 and -55 ppm, as previously mentioned by Quoirin.³⁷ Because of large linewidths, the two contributions severely overlap, yielding slightly asymmetric NMR centerband and sidebands. Perhaps easier to rationalize than the difference in isotropic positions of the two lithium contributions is the difference in widths of their spinning-sideband patterns (see Figure 7). As already mentioned, the width of the sideband pattern depends on the magnitude of the dipolar interaction of lithium nuclei with paramagnetic centers, which, in turn, depends on the distances between the nuclei and the centers. Inspecting the proposed structure of $P2_1/n$ polymorph,³⁸ one can distinguish two equally populated lithium sites. While the Li(2)O₄ tetrahedron shares corners with four neighboring

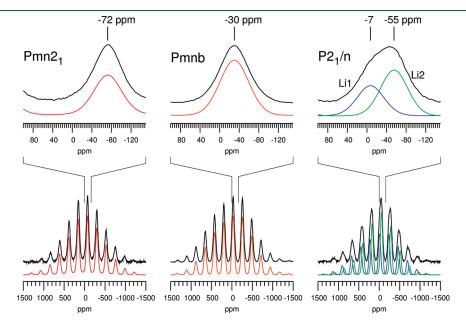


Figure 6. 6 Li MAS NMR spectra of $Pmn2_1$ (LFS@400 sample), Pmnb (LFS@900 sample), and $P2_1/n$ polymorphs (LFS@700 sample). The bottom part of the figure shows entire spectra with broad spinning-sideband patterns. The top part of the figure shows isotropic bands (centerbands) of the three spectra. Spectra of LFS@400 and LFS@900 can be well-fitted by a single Li contribution. The spectrum of LFS@700 can be described as a sum of two contributions; one is plotted in green, another in blue. Solid black lines represent measured spectra.

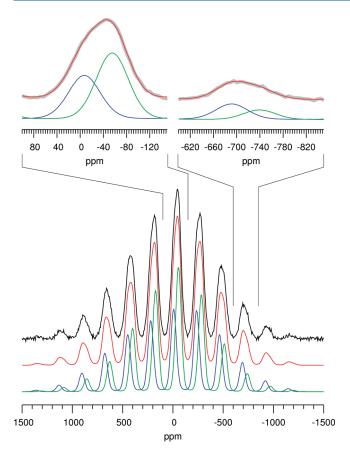


Figure 7. The decomposition of the 6 Li MAS NMR spectrum of the $P2_1/n$ polymorph (LFS@700) into two contributions. Although the centerbands and the sidebands of the two contributions overlap severely, they produce asymmetric peaks, which still allow relatively reliable decomposition (especially because the spinning-sideband patterns of the two contributions are differently broad and, thus, the "asymmetric shape of the peaks" changes with the rank of the sideband).

FeO₄ tetrahedra, the Li(1)O₄ tetrahedron shares corners with two and an edge with one of the neighboring FeO₄ tetrahedra (see Figure 3). The distances between Li and Fe sites in edgesharing tetrahedra are substantially shorter than the distances between lithium and iron sites in corner-sharing tetrahedra. The first amounts to \sim 0.28 nm and the second exceeds 0.3 nm. Because of the short distance, the interaction between Li(1) nuclei and iron centers is stronger, and the induced width of the NMR spinning-sideband powder pattern is larger. Tentatively, a narrower powder pattern with isotropic shift of -55 ppm can be assigned to the Li(2) site, and a broader powder pattern with isotropic shift of -7 ppm can be assigned to the Li(1) site.

The width and the shape of the spinning-sideband powder patterns can be assessed also more quantitatively. Nayeem and Yesinowski³⁹ showed that the effect of through-space dipolar interaction between the nuclear spin and several paramagnetic centers can be described by the Hamiltonian

$$H_{\rm en} = \hbar \gamma \mathbf{B}_0 \sigma_{\rm en} \mathbf{I} \tag{1}$$

where γ is the nuclear gyromagnetic ratio, B_0 the external magnetic field, and I the nuclear spin operator. The tensor

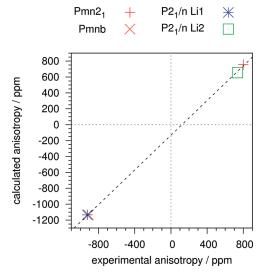


Figure 8. Calculation of tensors, describing through-space electron—nucleus dipolar interaction. The graph shows the correlation between the measured and the calculated dipolar-interaction anisotropy parameters for four Li sites in LFS polymorphs.

 $\sigma_{\rm en}$ can be expressed as

$$\sigma_{\rm en} = \frac{\mu_0}{4\pi} \left[\frac{\mu_{\rm B}^2 S(S+1)}{3kT} \right] \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{D}_{\rm en}$$
 (2)

where $\mu_{\rm B}$ is the Bohr magneton, S the spin of the paramagnetic center, and $\mathbf{D}_{\rm en}$ the dipolar matrix $(D_{\alpha\beta} = \Sigma_i (\delta_{\alpha\beta} - 3e^i_{\alpha}e^i_{\beta})/r_i^3)$, which contains only information about the positions of paramagnetic centers with respect to the nucleus. Other symbols have their usual meaning.

If we assume the g-tensor to be isotropic and equal to 2, we can verify if meaningful prediction of the spinning-sideband powder patterns of ⁶Li MAS NMR spectra can be obtained solely based on the geometrical information about the arrangement of Fe²⁺ ions around Li nuclei. We calculated the σ_{en} tensors for the Li sites of the $P2_1/n$, $Pmn2_1$, and Pmnb polymorphs, using the proposed structures and assuming that spin-delocalization is negligible. We took into account all the Fe sites within a sphere with a radius of 0.8 nm around a selected Li nucleus and estimated the effective magnetic moment using a theoretical Bohr magneton number for Fe²⁺ ions of 4.9,⁴⁰ anticipating that the crystal field was much stronger than the spin-orbit coupling. The calculated anisotropy parameters $\sigma_{\rm en}^{\rm aniso}$ are compared to the experimentally obtained values in Figure 8. The latter anisotropy parameters were actually extracted from ⁶Li MAS NMR spectra by using the simulations of spinning-sideband patterns (see the Supporting Information). In addition to the interaction with paramagnetic centers, the sideband patterns of ⁶Li MAS NMR spectra are affected also by electric quadrupolar interaction.⁴¹ Chemical shift anisotropy and nuclear dipole—dipole couplings are negligible and were not taken into account in the analysis of the sideband patterns. We also did not take into account the bulk magnetic susceptibility (BMS) effect. In diamagnetic materials, broadening due to BMS is usually rather small and is spun away by magic-angle spinning (MAS). 42,43 In paramagnetic materials, however, the BMS effect can be large and often cannot be entirely removed by MAS. In some cases, it can contribute substantially to sideband intensities. 41 Quantitatively, the BMS contribution

Table 3. NMR Parameters^a Obtained Via the Analysis of ⁶Li MAS NMR Spectra

	$\delta^{ m iso}$ [ppm]	$\sigma_{ m en}^{ m \ aniso} \left[m ppm ight]$	$\eta_{ m en}$	$\chi_{Q}\left[kHz\right]$	η_{Q}			
LFS@400	-72	800	1.0	24	1.0			
LFS@900	-30	-910	1.0	22	0.3			
LFS@700 Li1	-7	-920	1.0	21	0.2			
LFS@700 Li2	-55	740	1.0	24	1.0			
$ \begin{array}{l} ^{a}\sigma_{\rm en}^{\ \ iso} = {\rm Tr}\{\pmb{\sigma}_{\rm en}\}/3, \sigma_{\rm en}^{\ \ aniso} = \sigma_{\rm en}^{\ \ ZZ} - \sigma_{\rm en}^{\ \ iso}, \eta_{\rm en} = (\sigma_{\rm en}^{\ \ YY} - \sigma_{\rm en}^{\ \ XX})/\sigma_{\rm en}^{\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $								

to spinning-sideband pattern is, unfortunately, very difficult to assess, and its analysis exceeds the scope of this paper.

The results of the analysis of sidebands patterns, taking into account only electron-nucleus dipolar and electric quadrupolar interactions, are collected in Table 3. The above-mentioned approximations, especially the neglected BMS effect, might be responsible for the slight disagreement between the measured and the simulated NMR spectra (see the Supporting Information). Because of that, the anisotropy parameters extracted by the analysis of spinning-sideband intensities can be considered more as estimates than as precisely measured values. Nevertheless, they still correlate well with the predicted anisotropy parameters and can be rationalized by the differences in the symmetry of the local Li environments. The Li site of $Pmn2_1$ and Li(2) site of $P2_1/n$ polymorphs are surrounded by four Fe²⁺ ions that are sitting in the corners of slightly distorted tetrahedra. Such relatively symmetric environments lead to quite small electron-nucleus anisotropy parameters. The Li(1) site of the $P2_1/n$ polymorph and the Li site within the Pmnb polymorph are both bonded to only three ${\rm Fe}^{2+}$ ions and occupy less-symmetric positions slightly above triangles of ${\rm Fe}^{2+}$ ions. Li on these sites experiences larger anisotropy of electron-nucleus dipolar interaction. Very similar differences in $\sigma_{
m en}^{
m aniso}$ were observed already for Li nuclei surrounded by either four or three Mn2+ ions within the Li₂MnSiO₄ polymorphs. 16 The magnitudes of the anisotropy parameters in LFS and LMS materials are also comparable, suggesting that the BMS effect does not dominate the spinningsideband patterns. Most likely, it affects only intensities of the lowest-rank sidebands (zeroth, first, second), which is probably why the fitting/simulation process in all Li₂FeSiO₄ polymorphs converged to an asymmetry parameter value of $\eta_{\rm en}$ = 1.

As in the case of Li₂MnSiO₄, the anisotropy parameters thus again reflect the short-range structural motifs of the polymorphs and enable the assignment of two detected NMR contributions to two Li sites of the $P2_1/n$ polymorph. However, the anisotropy parameters of the Li site of the Pmnb polymorph and the Li(1) site of the $P2_1/n$ polymorph hardly differ from each other. This means that, based only on $\sigma_{\rm en}^{\rm aniso}$, we cannot distinguish between the two Li environments. In contrast, although the centerbands are relatively broad, we can still distinguish different isotropic shifts for the four different Li sites within the three polymorphs. In the case of the Li₂MnSiO₄ polymorphs, the isotropic shifts were determined by the strength of hyperfine coupling of lithium nuclei with unpaired electronic spins. The hyperfine coupling constants were successfully predicted by the DFT Projector-Augmented-Wave (PAW) approach, ¹⁶ and

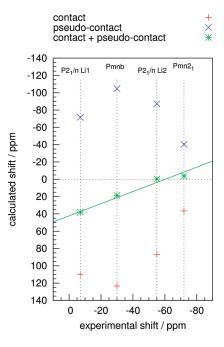


Figure 9. Correlation between the measured and the calculated (using DFT with either PAW or GIPAW reconstruction) contact, pseudocontact, and total isotropic shifts due to electron—nucleus hyperfine and dipolar interactions in LFS polymorphs.

the isotropic shifts obtained from them agreed well with the measured values.

Along the same lines as those for the Li₂MnSiO₄ polymorphs, we tried to reproduce the measured isotropic shifts by theoretical calculations also for Li₂FeSiO₄. However, with the available normconserving pseudo-potentials and within the implemented generalized gradient approximation of Perdew-Burke-Ernzerhof (GGA PBE), the calculated contact (hyperfine) isotropic shifts for all four different Li sites were small and positive. In addition to potential limitations in the accuracy of the first-principles calculations, the discrepancy between the measured and the calculated isotropic shifts in iron-containing paramagnetic materials also could stem from the so-called "pseudo-contact" shift. Such a shift can be expected when the magnetic susceptibility of a material is anisotropic. Because the anisotropy of the magnetic susceptibility or the anisotropy of the g-tensor could not be measured in the powdered LFS polymorphs, we again used the GIPAW module of the Quantum Espresso code²⁹ to predict the anisotropy of the g-tensor from first principles³¹ (based on known crystal structures). When the g-tensor was obtained, it was inserted into eq 2, and the isotropic pseudo-contact shift was then simply calculated as

$$\delta^{PC} = \frac{1}{3} Tr\{\sigma_{en}\} \tag{3}$$

Afterward, the total isotropic shift was obtained as a sum of two contributions: a contact shift and a pseudo-contact shift.

The results of calculations are presented in Figure 9. In all cases, the pure pseudo-contact shift for lithium nuclei was negative. The magnitude of the pseudo-contact shift was comparable to the magnitude of the contact shift. Although the sum of two contributions in only one case led to a negative total isotropic shift, and in three cases led to slightly positive isotropic shifts, the correlation with the measured values is still fine. More

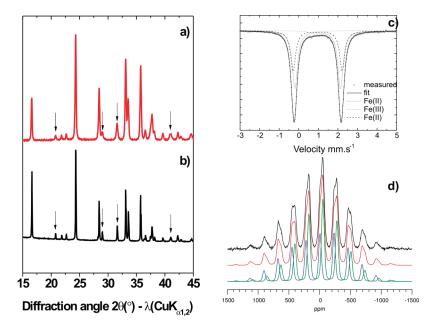


Figure 10. (a) Powder XRD pattern, (b) simulated XRD pattern (space group $P2_1/n$), (c) ⁵⁷Fe Mössbauer spectrum, and (d) ⁶Li MAS NMR spectrum of the battery sample.

importantly, these calculations prove that, in the case of LFS materials, pseudo-contact shifts induced by the anisotropy of the g-tensor are not negligible and substantially contribute to the total isotropic shift. The calculations also show that rough quantitative estimations of pseudo-contact shifts are possible. To the best of our knowledge, this is the first quantitative analysis of pseudo-contact paramagnetic shifts in lithium-based materials.

Quite expectedly, analogous calculations on Li₂MnSiO₄ polymorphs show that the g-tensor anisotropy is negligible in these materials. Since the g-tensor anisotropy is directly related to the anisotropy of magnetic susceptibility, it seems reasonable that extensive broadening of centerbands and sidebands observed in 6Li NMR spectra of Li₂FeSiO₄, but not in the spectra of the Li₂MnSiO₄, is produced by this broadening mechanism. Note the difference between the previously discussed BMS effect and the just-mentioned anisotropic bulk magnetic susceptibility (ABMS) effect. The former (BMS) is larger and is important, even when the magnetic susceptibility tensor is isotropic. It does not affect the width of the centerbands and the sidebands, but, if strong enough, it can affect the intensities of the sidebands (i.e., it can affect the spinning-sideband pattern). The latter (ABMS) mechanism is effective only when the magnetic susceptibility tensor is anisotropic. In that case, the ABMS tensors of randomly oriented crystallites around a given crystallite generate a local magnetic field ,which varies from crystallite to crystallite in the sample. This means that ⁶Li nuclei in different parts of the sample resonate at slightly different frequencies, leading to inhomogeneous line broadening of centerbands and sidebands.

We can roughly estimate the contribution of the ABMS to the width of the NMR signals. VanderHart showed that, for an axially symmetric ABMS under MAS, the NMR frequencies are spread between $2\pi(\chi_{||}-\chi_{\perp})/3$ and $-\pi(\chi_{||}-\chi_{\perp})/3$. Here, χ and χ_{\perp} are the parallel and perpendicular components of the volume magnetic susceptibility tensor, respectively. For the LFS@900 sample, for which the calculated g-tensor is almost axially symmetric, the calculated difference $\pi(\chi_{||}-\chi_{\perp})/3$ is equal to

37 ppm. This confirms that linewidths of 60-70 ppm, as detected in LFS samples, indeed stem from ABMS broadening. Unfortunately, linewidths of the ⁶Li MAS NMR signals cannot be assessed entirely quantitatively. The extent of the ABMS broadening, namely, does not depend only on the difference $\chi_{\parallel} - \chi_{\perp}$, but also on the shape, size, and the packing of the crystallites.

■ CARBON-COATED Li₂FeSiO₄ SAMPLE

As an example of the application of the above-described spectroscopic techniques for the analysis of more-demanding materials, a carbon-coated Li₂FeSiO₄ sample ready for the electrochemical characterization was studied. The sample was prepared by heat treatment at 700 °C, followed by slow cooling to room temperature. Basically, it can be described as a LFS@700 sample, because its XRD pattern (Figure 10a) is very similar to the pattern of the $\text{Li}_2\text{FeSiO}_4$ crystallized in the $P2_1/n$ space group (simulated pattern is shown in Figure 10b). Hardly observable differences between patterns are observed, only in the width (fwhm) of the diffraction peaks typical for the LFS@700 phase (see arrows in Figures 10a and 10b). These "imperfections" in the XRD pattern are much more pronounced in the Mössbauer spectrum (Figure 10c). The fit of the spectrum shows that some of the iron (58 at. %) has a similar environment as the iron in the LFS@700 sample, whereas another major portion of iron (40 at. %) exhibits a QS parameter close to that of the LFS@400 phase and the IS parameter is still similar to that of the LFS@700 sample. This indicates that phase transformation from the $P2_1/n$ polymorph to the *Pmn*2₁ polymorph started but had not yet been completed. A similar conclusion can be drawn from the NMR spectrum of the carbon-coated sample (Figure 10d). The spectrum can be described as a sum of two contributions with very similar environments to those of the pure LFS@700 phase. However, the ratio of populations of the two Li sites now deviates from 1:1 and amounts to 0.8:1 (Figure 10d). This suggests that the local environment of a substantial part of the lithium started to change.

■ CONCLUSIONS

We showed that ⁵⁷Fe Mössbauer and ⁶Li MAS NMR spectra were very sensitive to the local environment of cations in Li₂FeSiO₄, and that the parameters obtained from these spectra were giving typical values for each of the crystallographically pure Li₂FeSiO₄ polymorphs.

The polymorphs differ in the connectivity and in the orientation of the tetrahedra, which, together, affected the average Fe-O bond lengths, the distortion of the FeO₄ tetrahedra, and the connectivity scheme between LiO₄ and FeO₄ tetrahedra. Consequently, shorter Fe—O bonds (stronger covalent nature) give rise to smaller chemical shifts in the Mössbauer spectra. Average Fe-O bond lengths decrease as the temperature used for the isolation of a particular polymorph increases (i.e., the shortest bonds were detected in LFS@900 sample). The asymmetry parameter of the electron-nucleus dipole-dipole interaction, which could be obtained via an analysis of spinningsideband patterns of ⁶Li MAS NMR spectra, depended on the arrangement of Fe²⁺ ions around ⁶Li nuclei. By inspecting the sideband pattern, we could easily discriminate between Li NMR signals that belong to those LiO₄ tetrahedra that only share corners with neighboring FeO₄ tetrahedra, and those LiO₄ tetrahedra that also share an edge with one of the neighboring FeO₄ tetrahedra. Analysis of ⁶Li NMR isotropic shifts was the most demanding. The magnitude and the sign of the shift could not be plainly related to the geometrical description of the lithium local environment; the relationship between the structure and the isotropic shift was established only by using quantum-mechanical calculations. In the present case of Li₂Fe-SiO₄ polymorphs, the isotropic shifts were composed of the contact and the pseudo-contact shift. Based on known structures, both of them were estimated by DFT-based first principles calculations. The calculation of the pseudo-contact shift required knowledge of the components of the g-tensor, which were calculated ab initio, using the DFT/GIPAW approach. In Li₂FeSiO₄ polymorphs, the pseudo-contact shifts were of comparable amplitude but opposite sign as the contact shifts. The anisotropy of the g-tensor also was responsible for severe broadening of the NMR signals, which cannot be removed by magic-angle spinning (MAS). This broadening and the substantial pseudo-contact shift make the analysis of ⁶Li MAS NMR spectra of Li₂FeSiO₄ polymorphs much more demanding than the analysis of NMR spectra of Li₂MnSiO₄ polymorphs. Spectroscopic investigation of pure Li₂FeSiO₄ polymorphs, and the knowledge gathered in this way, simplified the analysis of carbon-coated Li₂FeSiO₄ sample (i.e., it enabled easy identification of deviation from the pure structure).

ASSOCIATED CONTENT

Supporting Information. This material is available free of charge via the Internet at http://pubs.acs.org.

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■ ACKNOWLEDGMENT

The financial support from the Ministry of Education, Science and Sport of Slovenia, the Slovenian Research Agency, EN-FIST

Centre of Excellence, and CO-NOT Centre of Excellence and the support from the ALISTORE European Research Institute (ERI) are acknowledged. The Ministère de l'Enseignement Supérieur et de la Recherche, France, is acknowledged for supporting CS through an International PhD Student Scholarship shared between Amiens (France) and Ljubljana (Slovenia). Matthieu Courty (LRCS) is thankfully acknowledged for performing the TG/DSC measurements.

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